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A REVIEW ON SOME THEORETICAL AND EXPERIMENTAL INVESTIGATIONS ON NANOFLUIDS

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Abstract:

Past few decades, nanotechnology plays an important role to overcome the usage of traditional materials by improving the multifunctional material complex models. In the last two decades, the researchers have shown a keen interest on developing the complex models on nanofluids by considering the different particles or shapes or sizes with different designs. This review summarizes the theoretical and experimental investigations and developments in nanofluids

Keywords: Convection, Nanofluids, Nano particles, Heat transfer, MHD.

Introduction:

Nanofluid is not only the mixture of liquid-solid alloys. It is also having some special characteristics like stable suspension, durability and collection of particles. Nanofluids are the suspensions of the nano meter sized metallic or nonmetallic powders into base fluids. Fig.1 shows the pictorial presentation of the preparation of a nanofluid and cross section of nanofluid structure consisting of nano particles.

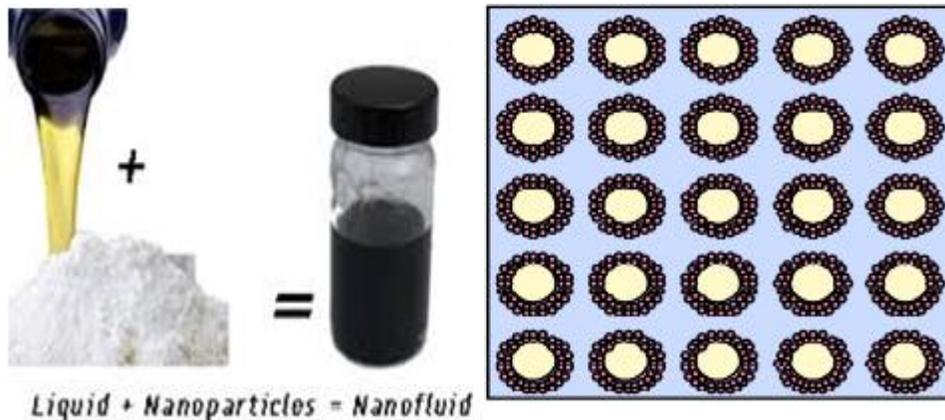


Fig.1 Preparation of nanofluid and its structure.

Convectional base fluids contain mm or micro meter sized particles. Due to this reason, the thermal conductivity of the convectional base fluids has inherently poor while compared with the solids. The suspension of nano powders into convectional base fluids helps to enhance the heat transfer rate. Table 1 depicts the materials for base fluids and nano particles.

Table.1: Materials for base fluids and nano particles.

Base Fluids	Nanoparticles material
Water	Oxide Ceramics - CuO, Al ₂ O ₃ ,ZrO ₂ ,TiO ₂
Ethylene or try-ethylene glycols	Metals – Al, Cu, Zn, Ag
Polymer solutions	Nitrides – AlN, SiN
Bio fluids	Metal Carbides – SiC
Oil and other lubricants	Non-metals – Graphite , carbon nanotubes
Other common fluids	Phase change materials and Functionalized nano particles

Around 120 years ago, Maxwell [1] was the first person who discussed about the suspension of the particles into the liquids. He suspended the large size and high density particles into base fluids. Due to the stability variations in the suspension, there exists an erosion and additional flow resistance. This fails to prevent the solid particles from the suspension. Further in 1915, Ostwald [2] was the first person who discussed about the properties of nano particles including its shape, size and colour. The next generation of heat transfer in fluids suspended by particles was started with Choi [3] in Argonne National Laboratory, U.S.A. He suspended nano meter sized particles into convectional base fluids and named it as “Nanofluid”. He observed a significant enhancement in the heat transfer performance due to the suspension of the nano particles into base fluid. He also observed the increase in the stability of suspensions. Due to the fascinating thermal characteristics of nanofluids, this research has attracted a vast interest from the researchers worldwide. Lu and Lin [4] extended the basic model of Maxwell [1] by considering the spheroidal suspensions into the convectional flows and observed a rise in the heat transfer performance of the combined fluid. By using Boltzmann model Chen [5] observed depreciation in conductivity of nanofluid for nonlocal conduction and concluded that Boltzmann model fails to observe the enhancement in nanofluid conduction. In continuation of this Artus [6] studied the measurement of heat conduction by considering the prophoritic paste with heat sink.

Eastman et al. [7] investigated the heat transfer characteristics of nanofluids and found that the heat transfer enhancement in nanofluid is due to the larger surface area of nano particles. They also proved that there is 60% enhancement in thermal conductivity of water based nanofluid with the suspension of 5% volume of CuO nano particles. In continuation

of this study Wagener et al. [8] developed a direct condensation process. Pak and Cho [9] investigated the heat transfer characteristics of magnetohydrodynamic flows immersed with spherical shaped metallic oxide Al_2O_3 and TiO_2 nano particles and found 30% heat transfer enhancement in nanofluid while compared with the base fluid. The basic principles of gas-solid interaction flows were discussed by Fan and Zhu [10]. Lee et al. [11] proposed a new concept for measuring the thermal conductivity of the convectional base fluids embedded with the oxide nano particles and found a significant increase in the heat transfer rate of the mixed fluid. With the extension of the above work, Wang et al. [12] investigated the thermal conductivity of the nanofluid by considering the ethylene glycol based copper oxide nano particles and found a noticeable enhancement in the heat transfer rate of a nanofluid. Whitaker [13] proposed a new method for investigating the volume averaging of the nanofluids. Fig.2 displays the power density of the nanofluids and water. It is clear that the nano fluids have high power density while compared with the water.

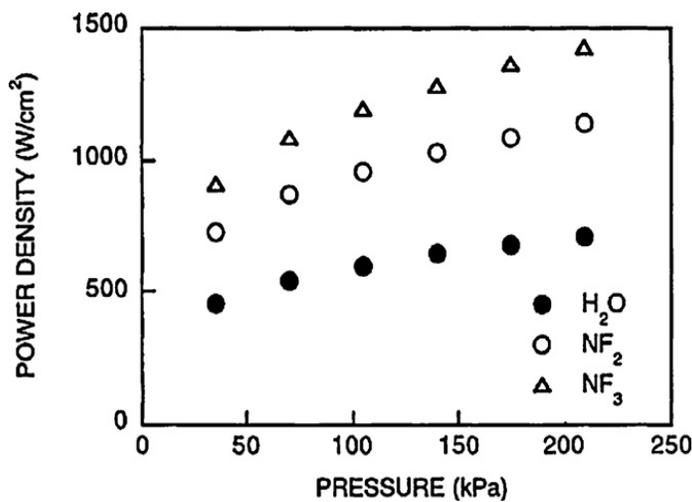


Fig.2 Power density with pressure for water and nanofluids [39]

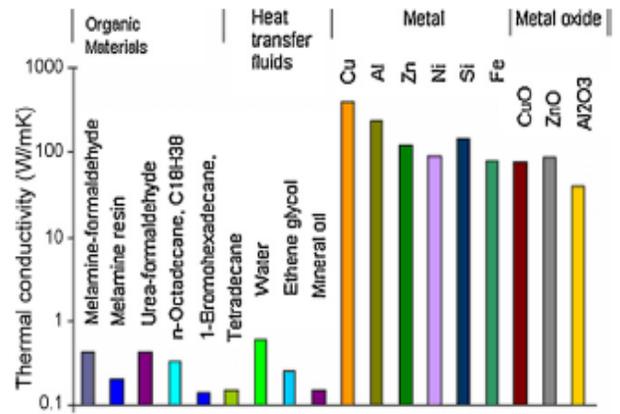


Fig.3 Thermal conductivity of some typical materials and base fluids [40]

For filling the gap between the results of theoretical and experimental data Eastman et al. [14] presented the thermal properties of the nano structured materials. Rise in the heat transfer coefficient also enhances the heat transfer rate. To enhance the heat transfer coefficient there is a need of adding the solid particles to the liquid coolants. The enhancement in the heat transfer rate due to the addition of nano meter sized particles was clearly described by Xuan and Roetzel [15]. With this inspiration Xuan and Li [16] analyzed the heat transfer characteristics of nanofluids and found a good enhancement in the heat transfer rate of nanofluid. High thermal conductivity of the nano tubes by considering the carbon and copper nano tubes were experimentally investigated by Berber et al. [17]. Eastman et al. [18] studied the heat transfer characteristics of the copper nano particles embedded ethylene glycol based nano fluid and found a gradual

enhancement in the heat transfer rate of the mixed fluid. In continuation of the above work Choi et al. [19] analyzed the heat transfer characteristics of the nanofluid by considering the different types of nano fluids and found a large improvement in effective thermal conductivity of the fluids containing metallic nano particles. Fig.3 displays the thermal conductivity of some typical materials and base fluids.

The researchers [20-23] analyzed the heat transfer characteristics of nanofluid embedded with the alumina, silicon and copper oxide nano particles and found that copper oxide mixed nanofluid is effectively enhances the heat transfer rate while compared with the other two nanofluids. The pool boiling and colloidal suspensions of various nanofluids by considering the different nano particles were discussed by the researchers [24-27]. Faulkner et al. [28] studied the forced convection flow of a nanofluid and concluded that the heat transfer enhancement in the forced convection flow of a nanofluid is comparatively better than the heat transfer enhancement in the free convection flow of a nanofluid. The researchers [29-30] experimentally investigated the heat transfer in nanofluids at the entrance region and inside the hydraulic diameter flat tube. To enhance the heat transfer rate of nanofluids, the researchers [31-32] analyzed the heat transfer rate of nanofluid by considering the flow through carbon nano tubes and flow through the rotary blade coupling. In addition with this, the researchers [33-34] proved that the shape of the nano particle and Brownian motion effect also plays major role while improving the heat transfer rate of the nano fluid. The enhanced heat transfer in TiO₂-water, Fe-water and Al₂O₃-water nanofluids was discussed by the researchers [35-40]. Fig.4 depicts the rate of heat transfer against the Reynolds number for laminar and turbulent flows. It is evident that the heat transfer rate in Al₂O₃-water nanofluid is highly significant in laminar flows. But Cu-water nanofluids are effectively enhances the heat transfer rate for turbulent flows.

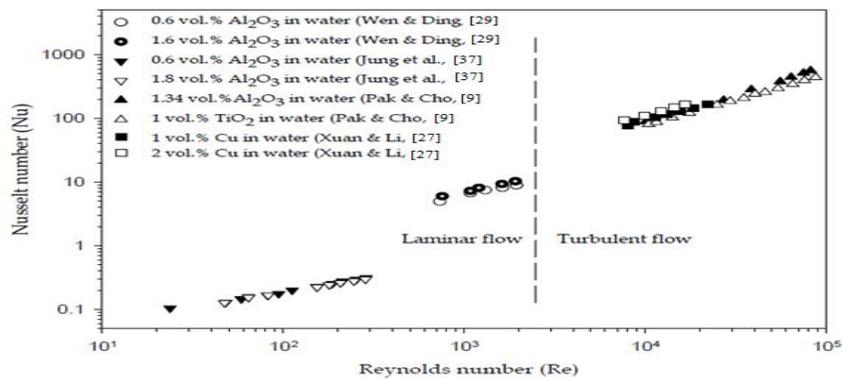


Fig.4 Convective heat transfer in nanofluids from various groups.

Applications:

Now a days the development in technology found in many areas like microelectronics, manufacturing and transportation, and has created a lot of ideas that have wide ranging influence on many problems facing today’s scientific world. However, there are many factors involves in further development in these areas, one of the big challenge is the rapidly cool the devices being used. Cooling is very important for the reliability of new products. The demand for efficient cooling devices has increasing dramatically in the last few decades. Consequently, more companies are started to invest the more capital into the research for finding the efficient heat transfer processes.

In 1996, for cooling the microchannel heat exchangers Lee and Choi [41] used the nanofluid as coolant. They found a gradual enhancement in the cooling rates while compared with the general base fluids like water, ethylene, oil etc. Finally, they concluded that the increase in cooling rate is due to the suppression or mixing of the nano particles. Nanofluids are also plays a key role in biological applications such as X-ray, DNA, RNA and fluids contained in nano pores etc. A clear description on biological applications of nanofluids was presented by [42, 43]

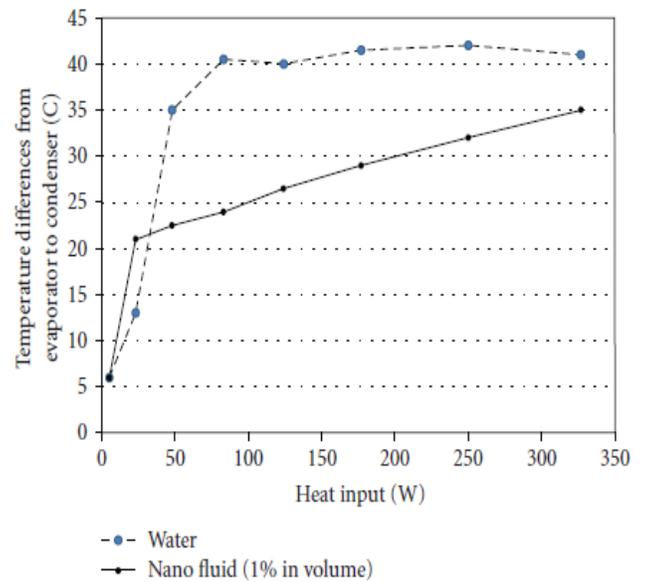
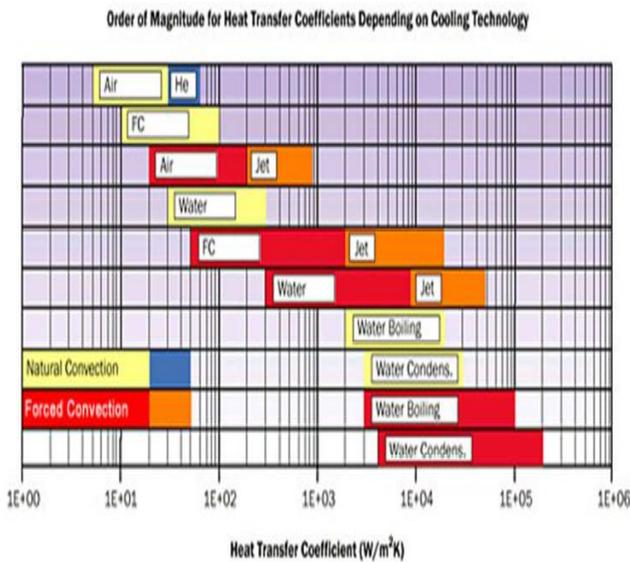


Fig.5 Heat transfer coefficients with different cooling technologies and fluids [44]

Fig.6 Nanofluid heat transfer capability [45]

Fig.5 illustrates the heat transfer coefficients with different cooling technologies and fluids. Sometimes heat source demands higher coefficients of heat transfer to fulfill the required cooling levels. In such situations free or forced convections plays a major role in cooling the devices. To enhance the heat transfer coefficient, different fluids have the different heat transfer properties. Based on the heat transfer coefficient levels of the base fluids, suitable nano mixtures

helps to further enhancement of the heat transfer coefficient levels and it can be applicable in many engineering and industrial sectors. Fig.6 shows the heat transfer capacity of nanofluid at different temperatures. It is clear that nanofluid have a good thermal conductivity at lower temperatures also. It is also noticed a huge temperature difference of the water from nanofluid. It is evident to mention that with an increase of 1% volume fraction we have noticed a significant enhancement in heat transfer. So, increasing in the volume fraction of nano particles boost up the temperature profiles of the nanofluid. This is very useful for the manufacturing industries and engineering.

Variable viscosity and thermal conductivity of alumina-water nanofluid on heat transfer in free convective nanofluid was studied by Abu-nada [58]. The researchers [59-63] studied the convective heat transfer in free and forced convective nanofluid flows by considering laminar and turbulent models. Enhanced convective heat transfer using graphene dispersed nanofluids was illustrated by [64]. Numerical investigation of single phase forced convection heat transfer characteristics of nanofluid in a double-tube counter flow heat exchanger was numerically studied by [65]. Numerical investigation of convective heat transfer of nanofluids under a laminar flow regime was presented by [66]. The researchers [67, 68] presented a review on the convective heat transfer in nanofluids. A review of boiling and convective heat transfer with nanofluids was studied by [69]. Numerical study of heat transfer enhancement in mixed convection flow along a vertical plate with heat source / sink utilizing nanofluid was studied by [70]. Experimental investigation of forced convective heat transfer coefficient in nanofluids was numerically investigated by the authors [71, 72].

Table.2: Summary of the experimental studies on thermal conductivity of nanofluids.

Authors	Size of the particles(nm)	Nanoparticles & Base Fluid	Observations/Findings
Lee et al. [11]	24.4, 38.4/ 18.6, 23.6	Al ₂ O ₃ /CuO+ Water/EG	4% volume of CuO+EG mixture 20% enhancement
Das et al. [38]	38.4/28.6	Al ₂ O ₃ /CuO+ Water	At 21 ⁰ C to 52 ⁰ C the conductivity is increased 2-4 times
Eastman et al. [7]	33/36/18	Al ₂ O ₃ /CuO/Cu+ Water/HE-200oil	5% volume of CuO in water 60% enhancement
Wang et al. [12]	28/23	Al ₂ O ₃ /CuO+Wat er/EG/PO/EO	3% volume of Al ₂ O ₃ +water mixture 12% enhancement
Xuan & Li [16]	100	Cu+water/Oil	successful suspension of relatively big metallic nanoparticles

Murshed et al.[35]	∅10□40,∅1 5	TiO ₂ /DW	33% & 30% enhancement at 5 vol % for ∅10□40 & ∅15
Xie et al. [20]	∅26,600	SiC+water/EG	15.8% enhancement at 4.2% vol for ∅26 SiC-Water & 22.9% at 4% vol for ∅600 SiC-Water
Hong et al. [36]	10	Fe+EG	18% enhancement for 0.55% vol Fe+EG mixture nanofluid
Liu et al. [31]	∅20-30	CNTs+EG/EO	12.4% for EG at 1% vol, 30% for EO at 2% vol

Table.3: Summary of the theoretical studies on thermal conductivity of nanofluids.

Authors	Mathematical Formula for thermal conductivity $\left(\frac{k_{nf}}{k_f}\right)$
Maxwell[17]	$\frac{k_p + 2k_f - 2\phi(k_f - k_p)}{k_p + 2k_f + \phi(k_f - k_p)}$
Hamilton and Crosser[18]	$\frac{k_p + (n-1)k_f - (n-1)\phi(k_f - k_p)}{k_p + (n-1)k_f + \phi(k_f - k_p)}$
Bruggemen[19]	$\frac{1}{4} \left[(3\phi - 1) \frac{k_p}{k_f} + (2 - 3\phi) + \frac{1}{4} \sqrt{\Delta} \right]$
Wasp [20]	$\frac{k_p + 2k_f - 2\phi(k_f - k_p)}{k_p + 2k_f + \phi(k_f - k_p)}$
Jeffrey [51]	$1 + 3 \left(\frac{k_p / k_f - 1}{k_p / k_f + 1} \right) \phi + \left(3 \left(\frac{k_p / k_f - 1}{k_p / k_f + 1} \right)^2 + \frac{3}{4} \left(\frac{k_p / k_f - 1}{k_p / k_f + 1} \right)^2 + \dots \right) \phi^2$
Davis[52]	$1 + \left(\frac{3(k_p / k_f - 1)\phi}{(k_p / k_f + 2) - (k_p / k_f - 1)\phi} \right) (\phi + f(k_p / k_f)\phi^2)$
Lu and Lin [53]	$\frac{k_{nf}}{k_f} = 1 + (k_p / k_f)\phi + b\phi^2$
Yu and Choi [54]	$\frac{k_{nf}}{k_f} = \frac{k_p + 2k_f - 2\phi(k_f - k_p)(1 + \beta)^3}{k_p + 2k_f + \phi(k_f - k_p)(1 + \beta)^3} S$
Patel [55]	$\frac{k_{nf}}{k_f} = 1 + \frac{k_p d_f \phi}{k_f d_p (1 - \phi)} \left[1 + c \frac{2k_B T d_p}{\pi \alpha_f \mu_f d_p^2} \right]$

Koo and Kleinstreuer [56]	$\frac{k_{nf}}{k_f} = \frac{k_p + 2k_f - 2\phi(k_f - k_p)}{k_p + 2k_f + \phi(k_f - k_p)} + 5 \times 10^4 \beta \phi \rho_f (C_p)_f \sqrt{\frac{k_B T}{d_p \rho_p}} f(T, \phi)$
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Augmentation of free convective heat transfer nanofluids in the presence of magnetic field and uniform heat generation / absorption was discussed by [73]. Effect of thermophoresis and Brownian motion on magnetohydrodynamic flow of nanofluid was studied by [74]. The researchers [75-80] studied the heat transfer characteristics of MHD nanofluid flows by considering various geometries. Numerical investigation of MHD effects on alumina water nano nanofluid flow and heat transfer in a semi-annulus enclosure using LBM was studied by [81]. Heat and mass transfer of unsteady natural convection flow of some nanofluids past a vertical infinite flat plate with radiation effect was illustrated by [82]. Pressure drop and convective heat transfer of water and nanofluids in a double-pipe helical heat exchanger a double-pipe helical heat exchanger was studied by [83]. Heat transfer enhancement in MHD nanofluid flows was studied by the researchers [84-90]. The effect of radiation, chemical reaction, viscous dissipation, MHD, thermophoresis, Brownian motion and cross diffusion on nanofluid flows by considering the various geometries was numerically investigated by the researchers [91-110]. Very recently, the researchers [111-123] analyzed the heat and mass transfer characteristics of magnetohydrodynamic nanofluid flows.

Future scope:

Nanofluids, i.e., well-dispersed metallic nanoparticles at low volume fractions in liquids, enhance the thermal conductivity of the mixture's over the convective base-fluid values. Thus, they are potentially useful for advanced cooling of micro-systems. Still, key questions linger concerning the best nanoparticle-and-liquid pairing and conditioning, reliable measurements of achievable knf values, and easy-to-use, physically sound computer models which fully describe the particle dynamics and heat transfer of nanofluids. Keeping this into view authors may study the enhanced heat transfer of nanofluids by embedding the conducting dust particles of micrometer size.

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